

**II B. Tech I Semester Supplementary Examinations, May - 2018**  
**MATHEMATICAL FOUNDATION OF COMPUTER SCIENCE**  
 (Com to CSE & IT)

Time: 3 hours

Max. Marks: 70

- Note: 1. Question Paper consists of two parts (**Part-A** and **Part-B**)  
 2. Answer **ALL** the question in **Part-A**  
 3. Answer any **FOUR** Questions from **Part-B**

**PART -A**

1. a) Construct truth table for the compound predicate:  $p \rightarrow (\neg q \wedge r)$  (2M)
- b) Draw the Hasse diagram for the power set  $(P(S), \leq)$ , where  $S = \{1, 2, 3\}$ . (3M)
- c) Write a note on  $\equiv$  operator in modular arithmetic. (2M)
- d) How many ways are there to arrange the letters of the word ENGINEERING? (2M)
- e) Solve the following recurrence relation using generating functions:  $a_n - 6a_{n-1} = 0$  for  $n \geq 1$  and  $a_0 = 1$ . (3M)
- f) A complete binary tree has 125 edges. How many vertices does it have? (2M)

**PART -B**

2. a) Show that the following statement is a tautology: (7M)  
 $(\sim P \wedge (P \rightarrow Q)) \rightarrow (\sim Q)$
- b) Using automatic theorem proving, show that: (7M)  
 $(P \vee Q) \wedge (Q \rightarrow R) \wedge (P \rightarrow M) = (R \vee M)$
3. a) Verify the following relation R on  $X = \{1, 2, 3, 4\}$  is an equivalence relation or not? Given  $R = \{(1, 1), (1, 4), (4, 1), (2, 2), (2, 3), (3, 4), (3, 3), (3, 2), (4, 3), (4, 4)\}$ . (7M)
- b) Given below the relation matrix,  $M_R$  of a relation R on the set  $\{a, b, c\}$ , find the relation matrices of  $R^2 = R \circ R$ ,  $R^3 = R \circ R \circ R$ . (7M)

$$M_R = \begin{bmatrix} 1 & 0 & 1 \\ 1 & 1 & 0 \\ 1 & 1 & 1 \end{bmatrix}$$

4. a) Explain different tests for primality. (7M)
- b) Prove that  $G = \{-1, 1, i, -i\}$  is an Abelian group under multiplication. (7M)
5. a) What are the applications of Binomial and Multinomial coefficients? (7M)
- b) In how many ways can you select at least one king, if you choose five cards from a Deck of 52 cards? (7M)
6. a) Verify by mathematical induction that  $a_n = A_1 n + A_2$  is a solution to  $a_n = d a_{n/d} + e$  where  $n = d^k$ . (7M)
- b) Write about partial fraction decomposition. (7M)
7. a) What is a cut vertex, cut set and bridge? Explain with suitable examples. (7M)
- b) Show that the maximum number of edges in a complete bipartiate graphs with n vertices is  $n^2/4$ . (7M)

